

Web-Based Interactive Analysis and Animation of Mechanisms

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A Web-based mechanism analysis and animation system is presented in this article. The system is developed in Ch, an embeddable C/C++ interpreter, and Ch Mechanism Toolkit. It allows users to solve complicated planar mechanism problems conveniently on-line. Users can input the required data to define a mechanism in a Web browser and then click a button for kinematic and dynamic analysis, graphical plotting, and animation for fourbar, crank-slider, geared fivebar, sixbar linkages and cam-follower systems. Examples are provided to illustrate its ease of use as well as its suitability for distance learning. The Web-based system for mechanism analysis and animation is available on the Web at <http://www.softintegration/webservices/mechanism/> [DOI: 10.1115/1.2161230]

1 Introduction

Due to the rapid advancement of computer technologies, computational methods for analysis and design of multibody mechanical systems are popular in engineering practice. General purpose software packages such as Automated Dynamic Analysis of Mechanical Systems (ADAMS), Dynamic Analysis and Design System (DADS), Working Model [1] were developed to solve complicated engineering design and analysis problems. Although these software programs are powerful, learning curves for these packages are quite steep because users are assumed to have full knowledge of the subject. Special purpose software packages such as the Linkage Interactive Computer Analysis and Graphical Enhanced Synthesis Package (LINCAGES) [2,3], WATT by Heron [4], and Simulation and Analysis of Mechanisms (SAM) by Artas [5] are available for the synthesis and analysis of planar mechanisms. The software package SYNTHETICA [6] can be used for synthesis of spatial mechanisms. Compared with general purpose software packages, these specialized packages are easier to use for mechanism design and analysis. However, these software packages were not intended for Web-based mechanism design and analysis. They are not suitable for use in a network computing environment.

The Web is the most popular medium for passing information because of its versatility across heterogeneous networks and different platforms. It is increasingly popular to use the Web for mechanism design and analysis. For example, cam-follower systems can be designed on-line by entering some design parameters through a Web browser [7]. Control systems can be designed and analyzed on line [8,9]. We have developed a Web-based interactive mechanism design and analysis system [10,11] based on Ch,

a C/C++ interpreter [12–14], and Ch Mechanism Toolkit [15]. Ch, conforming to the international C standard with extensions, contains all salient features of MATLAB for numerical and script computing. The Ch Mechanism Toolkit [15], developed in Ch, is significantly different from other software packages. The users are able to examine the available source code and demo programs provided within the toolkit. The Web-based mechanism design and analysis system, based on this toolkit, is ideal for rapid prototyping. It provides the users with a convenient means to quickly obtain solutions to many mechanism design problems. It is especially suitable for teaching and learning mechanism design and analysis. The Ch Mechanism Toolkit and Web-based system have been used as teaching tools in an undergraduate course “Computer-Aided Mechanism Design” at the University of California, Davis [16]. The Web-based mechanism design and analysis system allows them to verify their solutions quickly with numerical and graphical output as well as animation. The toolkit provides students with the opportunity to study and understand the algorithms and their software implementation for mechanism design and analysis. Additionally, students can use the toolkit’s high-level building blocks to develop their own software programs for solving complicated engineering analysis and design problems. For example, students were assigned to develop a complete program for analysis and animation of a Whitworth quick return mechanism [16]. Programs based on Ch and its Mechanism Toolkit for kinematic synthesis of mechanisms are available [17].

In this paper, the Web-based interactive mechanism analysis and animation system will be described. Section 2 presents the major features of the system. Section 3 describes the design of the user interface. Section 4 highlights the software implementation of the system. Section 5 demonstrates its applications with examples. Finally, Sec. 6 provides a summary of Web-based mechanism analysis and animation system. Although the Web-based mechanism analysis and animation system includes many planar mechanisms, only the fourbar linkage is used to illustrate the interface and applications. The ideas presented are applicable to all other mechanisms.

2 Features of the Web-Based Mechanism Analysis and Animation System

The Web-based mechanism design and analysis system incorporates many of the features available in the Ch Mechanism Toolkit. With the Web-based system, users can solve complicated mechanism problems using a Web browser without programming. Some tedious and often complicated processes, such as kinematic analysis of a fourbar linkage, can be performed on-line with ease. All the users have to do is to enter parameters in fill-out forms and submit these values for analysis.

Figure 1 shows the initial Web page for mechanism design and analysis on the Web. It contains links to other Web pages for analysis of various planar mechanisms. For example, clicking on the Fourbar linkage link leads to Fig. 2, the primary Web page for fourbar linkage analysis and animation.

Figure 2 shows the main Web page for fourbar linkage analysis, which is separated into three sections: fourbar linkage analysis, synthesis, and special fourbar linkages. The first section consists of links to many Web pages for performing various operations, such as position, velocity, acceleration, and force analysis. Options for plotting the coupler curve and transmission angle is also available for the fourbar linkage. The next section of the Web page is for fourbar linkage synthesis. The synthesis capability of the system is very limited in the current implementation. It can perform three position synthesis of fourbar linkages. Given three sets of angles for the input/output links of a fourbar, this feature can be used to calculate link lengths of the fourbar that satisfies the relation of the input and output links. The last section of Fig. 2 contains links leading to descriptions of special fourbar linkages such as Grashof, non-Grashof, straight line, quick return, and symmetrical linkages as well as singular configurations. There are

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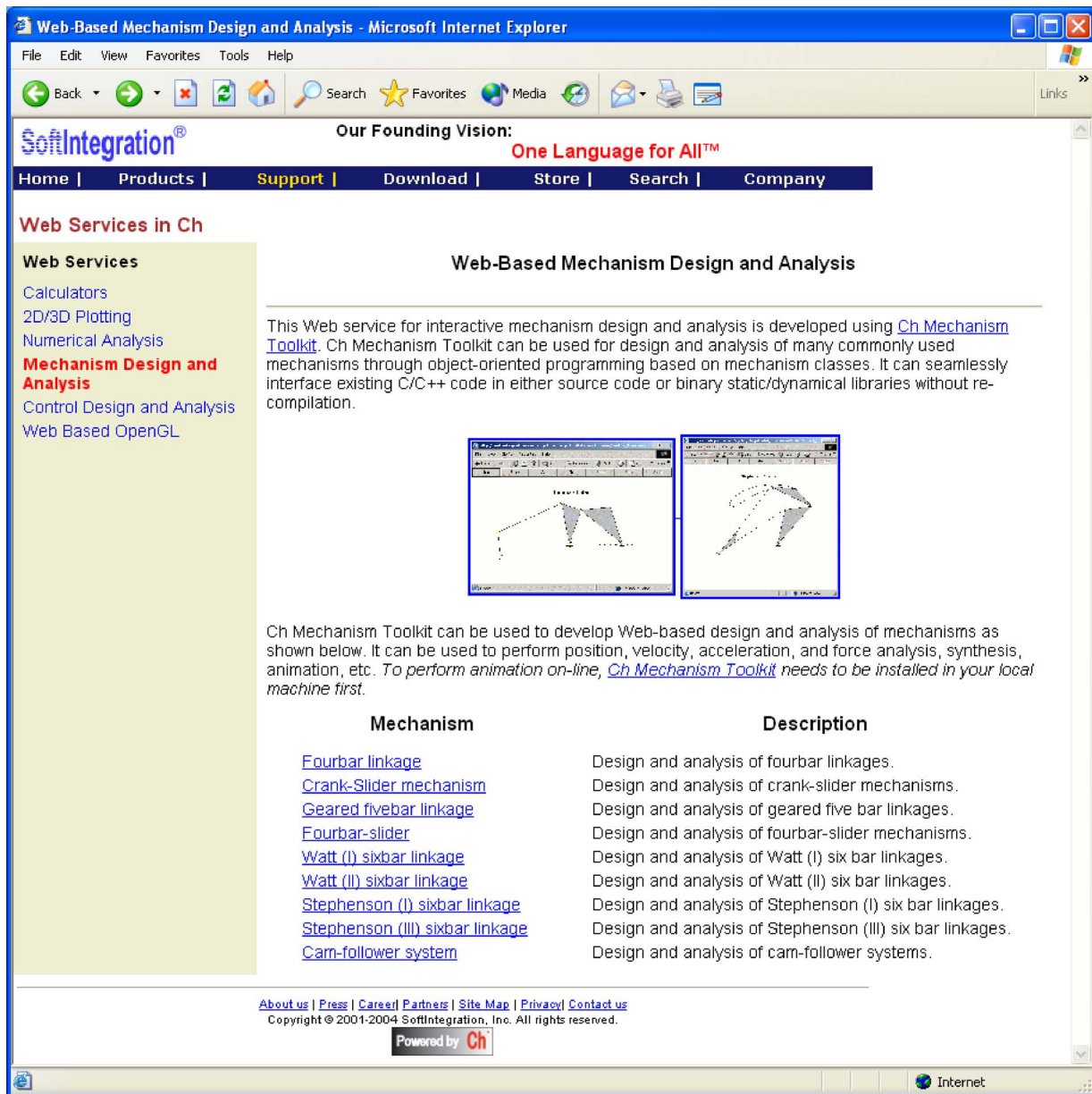


Fig. 1 The main Web page for mechanism design and analysis

a few variety of fourbars for the Grashof, non-Grashof, and straight line linkages. For example, Grashof linkages consists of the crank-rocker, rocker-rocker, rocker-crank, and crank-crank. Some example of straight line linkages are Burmester, Chebychev, Evans, Hoekens, Roberts, and Watt. The Web pages for these special fourbar linkages include a description of each type as well as an animation illustrating their characteristics. For example, the coupler curve for the mid point of the coupler of a Chebychev linkage is a straight line. The linkage has the constraints of $r_1:r_2:r_3=2:2.5:1$ and $r_3=r_4$.

Aside from the fourbar linkage, the Web-based mechanism system also contain tools for analysis of the crank-slider, geared-fivebar, various sixbar linkages, and cam-follower systems as shown in Fig. 1. The available sixbar models include the fourbar-slider, STEPHENSON (I) and (III) as well as WATT (I) and (II) sixbar linkages. Operations such as kinematic and dynamic analysis can be performed on the planar linkages mentioned above. For example, given a specific linkage configuration, the angular position, velocity, and acceleration for various linkages can be determined.

Similar to the Ch Mechanism Toolkit, the Web-based system also has some graphical features, such as the ability to simulate the motion of a given mechanism. This animation feature allows the user to visually study the behavior of the mechanism as it rotates through its entire range of motion.

3 User Interface for Web-Based Mechanism Analysis and Animation

The interface for the Web-based mechanism design and analysis system consists of a set of Web pages that the user may access to perform various operations. The Web pages were designed to be simple and easy to use. Useful description and implementation information are provided in each page, which are especially useful for learners. For example, Figs. 3 and 4 show the Web page for four bar angular position analysis. Given the angular position of one link, the angular position of the remaining links can be determined. Figure 3 and the top half of Fig. 4 contains a general figure of the fourbar mechanism along with the derivation for calculating

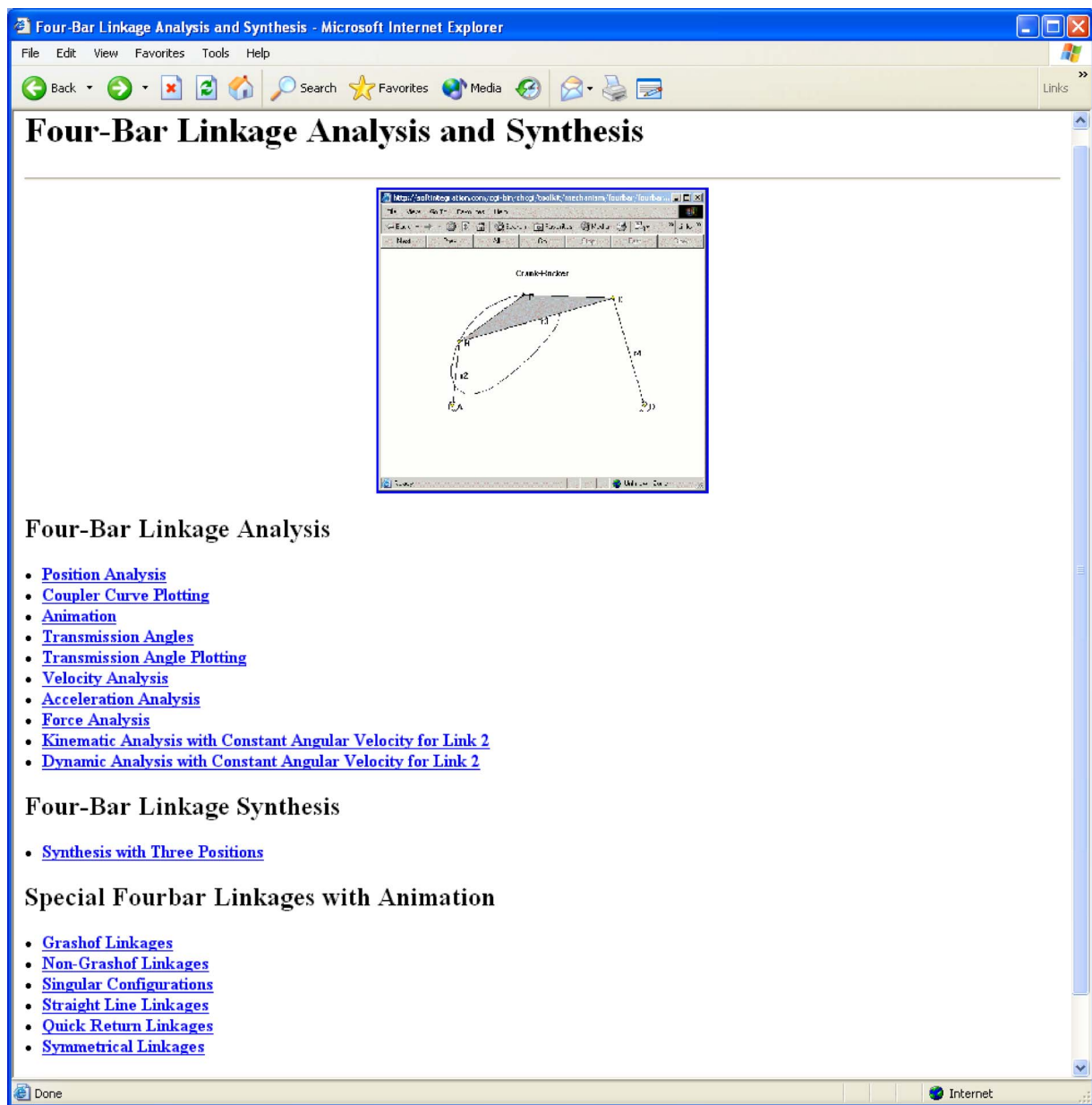


Fig. 2 The main Web page for fourbar linkage analysis and synthesis

the angular position values θ_2 , θ_3 , and θ_4 for links 2, 3, and 4, respectively. Following the derivation is the parameters section. It contains menu options and input boxes for the user to specify values required to perform the analysis. At the end of the page, two buttons, Run and Reset, allow the user to execute the analysis operation or reset the parameters back to their default values. The layout for the other Web pages for Web-based mechanism design and analysis is similar to the one shown in Figs. 3 and 4.

At the beginning of the parameter section of Fig. 4, the user has the option to choose U.S. Customary or SI units to specify the link lengths. Furthermore, the relevant angles may be specified in degrees or radians by selecting either Degree Mode or Radian Mode following the link length parameters. Figure 4 shows the default values for link parameters. Given the value of one angle from θ_2 , θ_3 , or θ_4 , this Web page can be used to calculate the value of the remaining two angles. As an additional option, the user may choose to have either a numerical or graphical output. If the first output option is selected, clicking on the Run button displays all the possible angular position values of the two unknown links.

Selecting the second output option allows the user to graphically display the current position of the fourbar mechanism. Note that the additional menu option is used to indicate which branch to display, since a fourbar linkage can have up to four branches.

4 Implementation of the Web-Based Mechanism Analysis and Animation System

As described in the previous section, the bottom of each analysis Web page consists of a Run and Reset button. The Reset button is used to return the input parameters back to their default values. Clicking on the Run button causes the Web-based mechanism design and analysis system to process the input data and output the desired result. This section describes the processes taking place when the Run button is clicked.

When the Run button is pressed on an analysis Web page, the parameters specified by the user are sent to the Web server. The information is passed via the Common Gateway Interface or CGI [18–20] through the POST method, which passes encoded field

Interactive Four-Bar Linkage Position Analysis - Microsoft Internet Explorer

File Edit View Favorites Tools Help

Back Forward Stop Home Search Favorites Media Mail Print

Interactive Four-Bar Linkage Position Analysis

Position analysis begins with formulating the loop-closure equation for the fourbar mechanism shown below.

$$r_2 + r_3 = r_1 + r_4 \quad (1)$$

Incorporating complex numbers,

$$r_2 \exp(i\theta_2) + r_3 \exp(i\theta_3) = r_1 \exp(i\theta_1) + r_4 \exp(i\theta_4) \quad (2)$$

Note link lengths r_1, r_2, r_3 , and r_4 along with θ_1 are constants. Let θ_2 be the independent variable, and θ_3 and θ_4 be the dependent variables. Rearranging the equation, we have

$$r_3 \exp(i\theta_3) - r_4 \exp(i\theta_4) = r_1 \exp(i\theta_1) - r_2 \exp(i\theta_2) \quad (3)$$

Let $R_1 = r_3$, $\phi_1 = \theta_3$, $R_2 = -r_4$, $\phi_2 = \theta_4$, and $z = (x_3, y_3) = r_1 \exp(i\theta_1) - r_2 \exp(i\theta_2)$. We now have a general complex equation

$$R_1 \exp(i\phi_1) + R_2 \exp(i\phi_2) = z \quad (4)$$

Angular positions θ_3 and θ_4 can now be solved for given parameters $r_1, r_2, r_3, r_4, \theta_1$, and θ_2 . From equation (4) we obtain

$$\cos(\phi_1) = (x_3 - R_2 \cos(\phi_2)) / R_1 \quad (5)$$

$$\sin(\phi_1) = (y_3 - R_2 \sin(\phi_2)) / R_1 \quad (6)$$

Fig. 3 Web-based fourbar position analysis

names and their associated values through the standard input file stream [21]. The CGI programs for Web-based mechanism design and analysis are written in Ch [14], Ch CGI [20], and Ch Mechanism Toolkit [15]. Ch Mechanism Toolkit performs the actual analysis prior to returning the desired output. Before any analysis can be performed, however, a CGI program has to sort out the data sent to it by the Web browser. One such sorting method is to use the `getForm()` function of class `CRequest` for CGI programming, which allows the program to obtain the value associated with the name indicated by the input argument of string type.

Once all the data have been sorted, an object of the appropriate mechanism class is created to begin the analysis process. The sorted data are then used as parameter values to specify the appropriate linkage mechanism (fourbar, crank-slider, or geared fivebar, etc.). Finally, the defined mechanism is evaluated, and the desired output is shown on the Web browser. Numerical outputs are automatically written into the browser window, whereas, the

data for plotting and animation are sent to the standard output stream. The Web browser receives the data and converts to the proper graphical output. Plots are initially generated using the `CPlot` class in the CGI programs and sent to the Web browser in Portable Network Graphics (PNG) file format. The animation data are generated in the same manner. However, it requires the QuickAnimation plug-in to display the animation in the Web browser window.

5 Examples of Web-Based Mechanism Analysis and Animation

In this section, two examples will be used to illustrate some of the features and applications of the Web-based mechanism design and analysis system.

5.1 Example 1. Problem Statement: The link lengths of a

Substituting these results into the trig identity $\sin^2(\phi_1) + \cos^2(\phi_1) = 1$ and simplifying we obtain

$$y_3 \sin(\phi_2) + x_3 \cos(\phi_2) = (x_3^2 + y_3^2 + R_2^2 - R_1^2) / 2 * R_2. \quad (7)$$

From this equation we can obtain formulas for ϕ_1 and ϕ_2

$$\phi_2 = \text{atan2}(y_3, x_3) \pm \text{acos}((x_3^2 + y_3^2 + R_2^2 - R_1^2) / 2 * R_2 * \text{sqrt}(x_3^2 + y_3^2)) \quad (8)$$

$$\phi_1 = \text{atan2}(\sin(\phi_2), \cos(\phi_2))$$

$$= \text{atan2}((y_3 - R_2 \sin(\phi_2)) / R_1, (x_3 - R_2 \cos(\phi_2)) / R_1). \quad (9)$$

Similar equations can be derived assuming either θ_3 or θ_4 is known with the other two angles as parameters.

Please enter link lengths, θ_1 and one other known angle to find the other two angles.

Unit Type:

Link lengths (m or ft): r_1 : r_2 : r_3 : r_4 : r_p :

Angles: θ_1 : β :

Select and input the known angle (θ_2 , θ_3 , or θ_4):

θ_2

Output option:

- Display angular position
- Display fourbar position -- Branch Number:


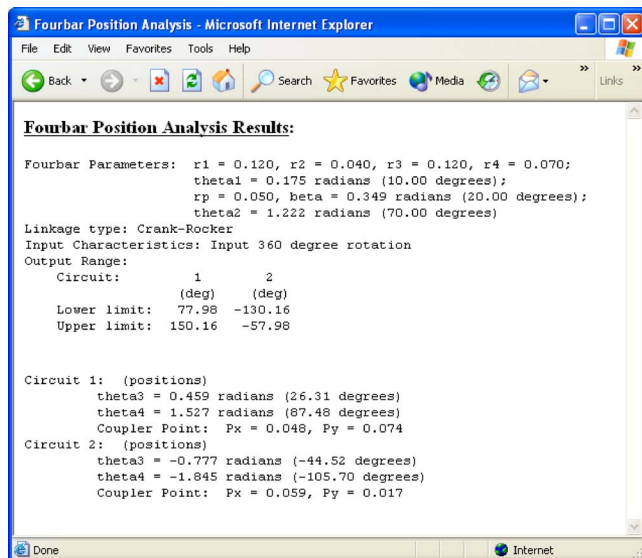
Powered by 

Fig. 4 Web-based fourbar position analysis (contd.)

fourbar linkage shown in Fig. 3 are given as follows: $r_1 = 12$ cm, $r_2 = 4$ cm, $r_3 = 12$ cm, and $r_4 = 7$ cm. The phase angle for the ground link is $\theta_1 = 10$ deg. The coupler point P is defined by the distance $r_p = 5$ cm and constant angle $\beta = 20$ deg. Determine the angular positions θ_3 and θ_4 as well as the position for coupler



Fourbar Position Analysis Results:

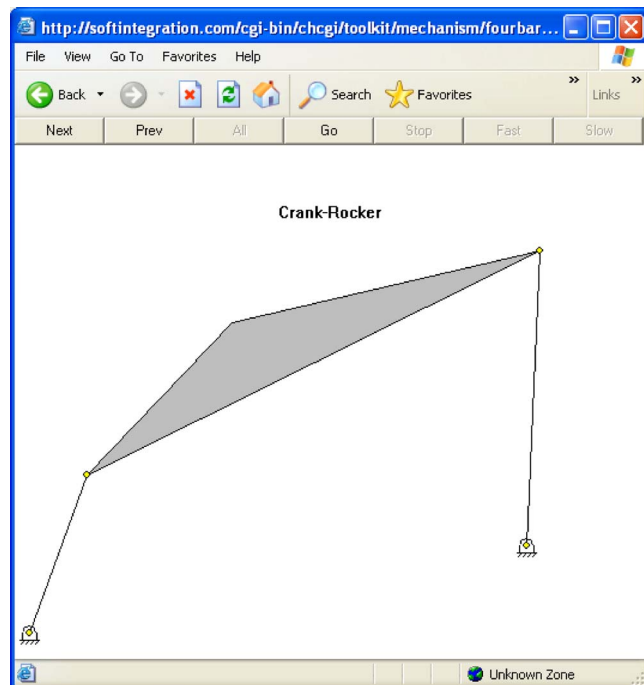
Fourbar Parameters: $r_1 = 0.120$, $r_2 = 0.040$, $r_3 = 0.120$, $r_4 = 0.070$;
 $\theta_1 = 0.175$ radians (10.00 degrees);
 $r_p = 0.050$, $\beta = 0.349$ radians (20.00 degrees);
 $\theta_2 = 1.222$ radians (70.00 degrees)

Linkage type: Crank-Rocker
Input Characteristics: Input 360 degree rotation
Output Range:
Circuit: 1 2
 (deg) (deg)
Lower limit: 77.98 -130.16
Upper limit: 150.16 -57.98

Circuit 1: (positions)
 $\theta_3 = 0.459$ radians (26.31 degrees)
 $\theta_4 = 1.527$ radians (87.48 degrees)
Coupler Point: $P_x = 0.048$, $P_y = 0.074$

Circuit 2: (positions)
 $\theta_3 = -0.777$ radians (-44.52 degrees)
 $\theta_4 = -1.845$ radians (-105.70 degrees)
Coupler Point: $P_x = 0.059$, $P_y = 0.017$

Fig. 5 Numerical output of the Web-based fourbar position analysis



http://softintegration.com/cgi-bin/chcgi/toolkit/mechanism/fourbar...

File View Go To Favorites Help

Back Prev All Go Stop Fast Slow

Crank-Rocker

Unknown Zone

Fig. 6 The graphical output for branch 1 of the Web-based fourbar position analysis

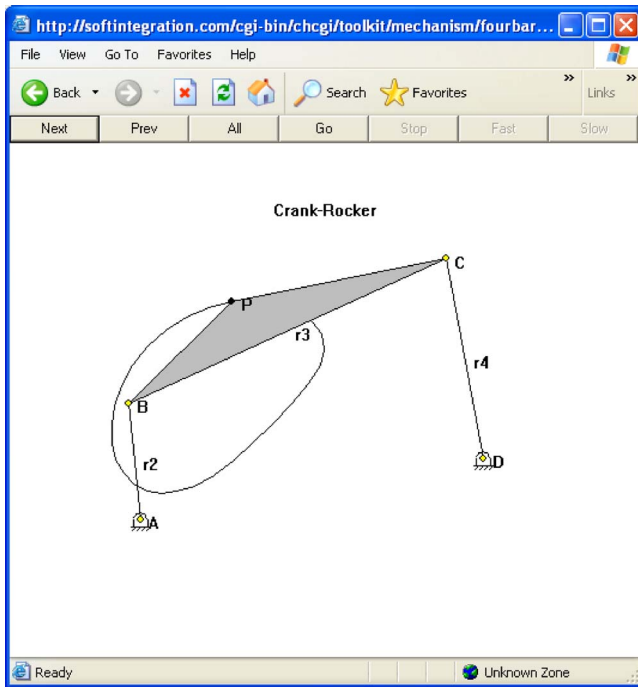


Fig. 7 The single frame of the Web-based fourbar animation

point P when the input angle $\theta_2 = 70$ deg.

This problem can be quickly solved by the angular position analysis Web page introduced earlier as shown in Fig. 4. After inputting the given parameters into the fill-out form, the analysis can be performed by simply clicking the Run button. The numerical results of the analysis are shown in Fig. 5. In addition to the values for θ_3 and θ_4 , the numerical output also displays the range of motion for the input/output links as well as the coupler point position P for each circuit of the fourbar. As shown in Fig. 5, the fourbar linkage is a crank-rocker with two circuits. The input

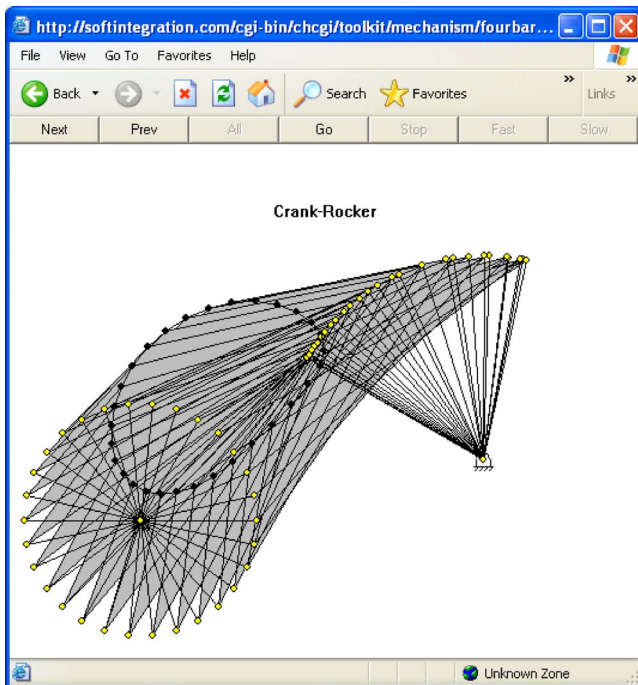


Fig. 8 All frames of the Web-based fourbar animation

range for θ_2 is a complete rotation with 360 deg. The output range for θ_4 is $77.98 \text{ deg} \leq \theta_4 \leq 150.15 \text{ deg}$ and $-57.98 \text{ deg} \leq \theta_4 \leq -130.16 \text{ deg}$ for the first and second circuits, respectively. At when θ_2 is 70 deg, θ_3 , θ_4 , and the coupler point are 26.31 deg, 87.48 deg, and (0.048 cm, 0.074 cm) for the first circuit and -44.52 deg , -105.70 deg , and (0.059 cm, 0.017 cm) for the second circuit, respectively.

If desired, the user may also choose to graphically display the configuration of the fourbar linkage, such as Fig. 6, which shows the configuration of the specified four bar for the first branch. Note that the four bar specified in the above problem statement is a crank-rocker, which means that there are two distinct circuits for each input link position. Thus, the user can display the second circuit by selecting 2 for the branch number prior to running the Web-based application in Fig. 4.

5.2 Example 2. Problem Statement: Simulate the motion of the fourbar linkage defined in Example 1 for its entire range of motion.

As in the first example, the above problem can easily be handled by the Web-based mechanism system. Similar to the four-bar position analysis Web page, the animation Web page also contains buttons, pull-down menus, and text boxes for users to specify the parameters of the fourbar linkage. The last option allows the user to indicate the branch number of the fourbar to animate. For typical fourbar linkages, such as the crank-rocker used in these two examples, there are two possible geometric inversions. However, for a fourbar rocker-rocker mechanism, there are a total of four possible geometric inversions. Figure 7 shows one frame of animation for the first geometric inversion of the fourbar crank-rocker mechanism, whereas Fig. 8 is an overlay of all the frames of the animation.

6 Conclusion

The Web-based mechanism analysis and animation system, based on the Ch Mechanism Toolkit, has been presented in this paper. This system consists of multiple user-friendly Web pages for the interface and CGI programs to perform the relevant analysis. The Web-based system is simple and easy to use. If the user ever enters an invalid value, an error message will be displayed to indicate the problem. The Ch Mechanism Toolkit and its Web-based extension can be used to solve various mechanism analysis problems. It can compute the angular positions, velocities, and accelerations of the individual links of mechanisms such as the fourbar, crank-slider, geared-fivebar, sixbar linkages, and cam-follower systems. Furthermore, it can also provide graphical output, such as animation, through the Web. The Ch Mechanism Toolkit and its Web-based system are not only useful for solving practical engineering problems, but also ideal for distance learning. The ideas and concepts presented in the Ch Mechanism Toolkit and Web-based system can be applied to solve many other mechanism designs and analysis problems.

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